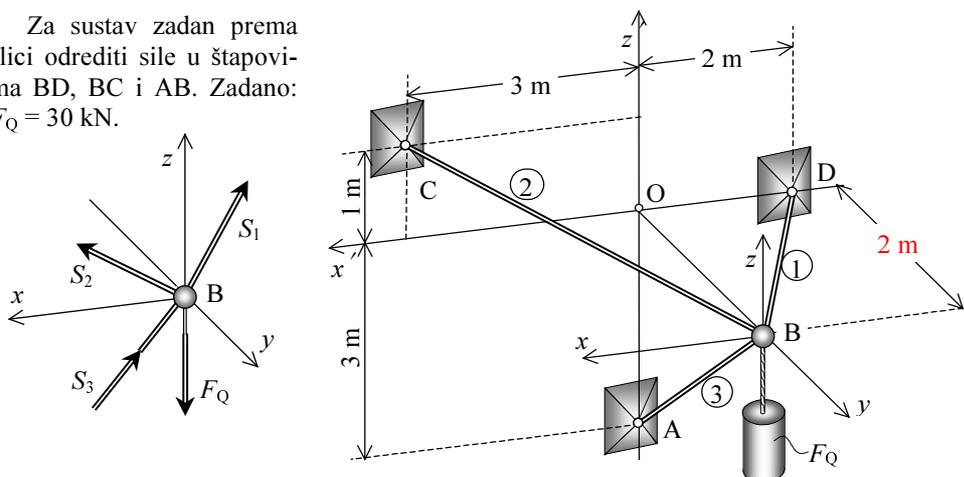


Primjer 4.1

Za sustav zadan prema slici odrediti sile u štapovima BD, BC i AB. Zadano: $F_Q = 30 \text{ kN}$.



Slika uz primjer 4.1

Rješenje:

Duljine štapova su: $\overline{BD} = 2\sqrt{2} \text{ m}$, $\overline{BC} = \sqrt{14} \text{ m}$, $\overline{AB} = \sqrt{13} \text{ m}$.

Ovdje se radi o konkurentnom skupu sila u prostoru te se sile u štapovima (koje se sve pretpostavljaju vlačne) mogu izračunati postavljanjem triju jednadžbi ravnoteže:

$$\sum F_x = 0, \quad -S_{1x} + S_{2x} = 0, \quad \frac{2}{2\sqrt{2}} S_1 = \frac{3}{\sqrt{14}} S_2, \quad S_1 = \frac{3\sqrt{2}}{\sqrt{14}} S_2,$$

$$\sum F_y = 0, \quad -S_{1y} + S_{2y} - S_{3y} = 0, \quad -\frac{2}{2\sqrt{2}} S_1 - \frac{2}{\sqrt{14}} S_2 - \frac{2}{\sqrt{13}} S_3 = 0,$$

$$\sum F_z = 0, \quad -S_{2z} - S_{3z} - F_Q = 0, \quad \frac{1}{\sqrt{14}} S_2 - \frac{3}{\sqrt{13}} S_3 - F_Q = 0,$$

$$S_3 = \frac{\sqrt{13}}{3} \cdot \left(-F_Q + \frac{S_2}{\sqrt{14}} \right).$$

Ako se izrazi S_1 i S_3 uvrste u jednadžbu 2) slijedi:

$$-\frac{1}{\sqrt{2}} \cdot \frac{3\sqrt{2}}{\sqrt{14}} \cdot S_2 - \frac{2}{\sqrt{14}} \cdot S_2 + \frac{2}{\sqrt{13}} \cdot \frac{\sqrt{13}}{3} \cdot \left(F_Q - \frac{S_2}{\sqrt{14}} \right) = 0,$$

$$S_2 = \frac{2\sqrt{14}}{17} \cdot 30, \quad S_2 = 13,21 \text{ kN}.$$

$$S_1 = \frac{3\sqrt{2}}{\sqrt{14}} \cdot \frac{2\sqrt{14}}{\sqrt{17}} \cdot F_Q = \frac{6\sqrt{2}}{17} \cdot 30, \quad S_1 = 14,95 \text{ kN}.$$

$$S_3 = -\frac{\sqrt{13}}{3} \cdot \left(F_Q - \frac{2\sqrt{14}}{17} F_Q \frac{1}{\sqrt{14}} \right) = -\frac{5\sqrt{13}}{\sqrt{17}} \cdot F_Q = -\frac{5\sqrt{13}}{17} \cdot 30, \quad S_3 = -31,81 \text{ kN}.$$